

# Weight Transfer and Traction



Course 4171

Material in this lecture was taken from chapter 16 of Gorring, Engine and Tractor Power, 1992

---

---

---

---

---

---

---

---

Figure 16.1

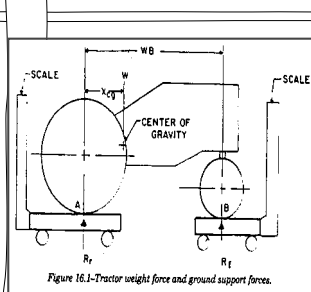


Figure 16.1- Tractor weight force and ground support forces.

Gorring, Engine and Tractor Power, 1992

- \* The center of gravity (CG) can be changed by adding a ballast.
  - A ballast ahead of CG increases  $X_{cg}$
  - A ballast behind CG decreases  $X_{cg}$
- \* Common ballast
  - Water with antifreeze in tire (25% air to absorb shock)
  - Rear wheel weights
  - Front end weights

---

---

---

---

---

---

---

---

## Center of Gravity

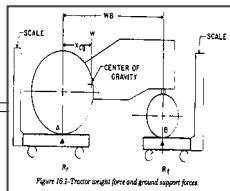


Figure 16.1- Tractor weight force and ground support forces.  
Gorring, Engine and Tractor Power, 1992

- \* Taking moment at A
- \*  $W * X_{cg} = R_f * W_B$
- \* Then,  $X_{cg} = (R_f * W_B) / W$  (lbs\*in)/lbs
  - Total weight known to be W
  - Front and rear wheel weight measured as Rf and Rb
    - $W_B$  = wheel base
    - $X_{cg}$  = center of gravity

---

---

---

---

---

---

---

---

## Weight Transfer

- \* Tractor can only produce drawbar load if ground provides a reaction force "Fc"
- \* The drawbar load  $F_{db}$  is shown at incline so  $Z_r$  and  $Z_f$  are different
- \* Choose moment about A
  - ▣ Change in front and rear wheel reactions as a result of drawbar load.

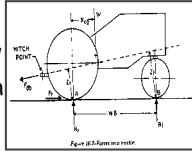


Figure 16.2 Forces on a tractor  
Goreing, Engine and Tractor Power, 1992

---

---

---

---

---

---

---

---

## Figure 16.2

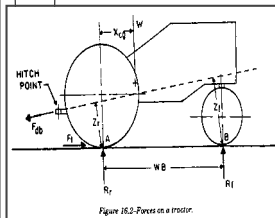


Figure 16.2 Forces on a tractor  
Goreing, Engine and Tractor Power, 1992

- \*  $R_f \cdot WB + F_{db} \cdot Z_r = W \cdot X_{cg}$
- ▣ Solve for  $R_f$  (Dynamic front wheel reaction)
- \*  $R_f = \frac{[(W \cdot X_{cg}) - (F_{db} \cdot Z_r)]}{WB}$
- \* Static front wheel reaction  
Let  $F_{db} = 0$  (no load)
- \*  $R_{f0} = (W \cdot X_{cg}) / WB$

---

---

---

---

---

---

---

---

## Weight Transfer for Inclined

$F_{db}$

- \* Front wheel:  $\Delta R_f = R_{f0} - R_f = (F_{db} \cdot Z_r) / WB$
- \* Rear wheel:  $\Delta R_r = R_r - R_{r0} = (F_{db} \cdot Z_f) / WB$ 
  - ▣ By choosing B as center of moment
  - ▣ For inclined load, the rear load increases more than the front load decreases
- \* For parallel load  $Z_r = Z_f$ , weight transfer >
  - $\Delta R_f = \Delta R_r$
  - ▣ Note: front end reaction is decreased the same amount rear end is increased.

---

---

---

---

---

---

---

---

# Tires

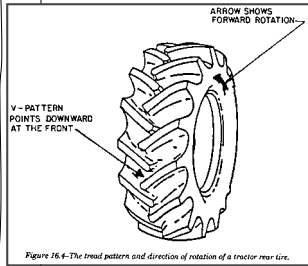


Figure 16-6-The tread pattern and direction of rotation of a tractor rear tire.  
Goring, Engine and Tractor Power, 1992

- # Rear tires - lugged to develop traction
- # Front tires - ribbed to improve steering
- # Types
  - ▣ Biased-ply
  - ▣ Radial-ply

---

---

---

---

---

---

---

---

# Types of tires

- # Biased-ply
  - ▣ Less expensive
- # Radial-ply
  - ▣ Lower pressure = more surface contact for better traction
  - ▣ Softer ride
  - ▣ More expensive
- # Dual tires - add contact area, reduce compaction, increase stress

---

---

---

---

---

---

---

---

# Traction

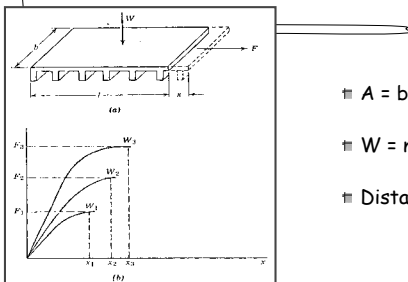


FIGURE 10-1 Method of determining maximum value of shearing force for various levels of vertical loading.  
Liljedahl, Tractors and Their Power Units, 1996

- ▣  $A = b \cdot l$  (footprint)
- ▣  $W =$  normal force
- ▣ Distance  $x$  is slip

---

---

---

---

---

---

---

---

## Theoretical Model of Tractive Force

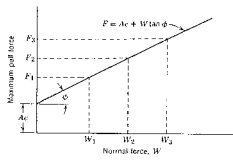


FIGURE 10-2 The soil parameters  $c$  and  $\phi$  can be determined from a plot of maximum values of the shearing force  $F$  versus the normal force  $W$ .

- ☒  $F = Ac + W \tan \phi$
- ☒  $F = A (c + p \tan \phi)$
- [10.2]
- ☒  $A = b * l$  (footprint)
- ☒  $c =$  soil cohesion
- ☒  $W =$  normal force
- ☒  $\phi =$  internal friction soil

Lijedahl, Tractors and Their Power Units, 1996

---

---

---

---

---

---

---

---

---

---

## Traction cont'

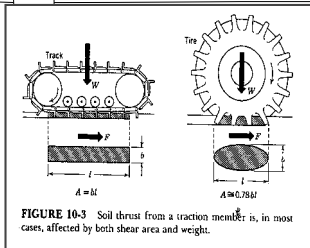


FIGURE 10-3 Soil thrust from a traction member is, in most cases, affected by both shear area and weight.

- ☒ Average soil pressure
- ☒  $P = W / (b * l)$
- ☒ For tire
- ☒  $P = W / (.788 * b * l)$
- ☒ However, we seldom know  $c$  and  $\phi$ , and  $p$  is not truly uniform.
- ☒ Alternate methods are needed

Lijedahl, Tractors and Their Power Units, 1996

---

---

---

---

---

---

---

---

---

---

## Definition

☒ A tractor can not develop drawbar power unless there is slip (travel reduction)

- ☒  $TR = 100 * [1 - (Sa/So)]$
- ☒  $TR =$  travel reduction
- ☒  $Sa =$  Actual speed, mph
- ☒  $So =$  speed without load on specific surface
- ☒  $Slip = 1 - (Sa/So)$
- ☒ Same as TR, only fraction

---

---

---

---

---

---

---

---

---

---

## Dynamic Traction Ratio

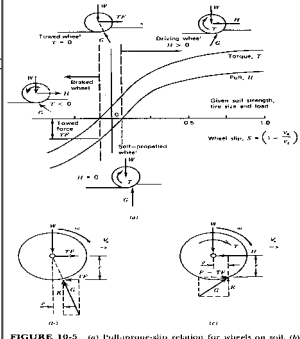


FIGURE 8B-3 (a) Pull-versus-slip relation for wheels on soil, (b) free-body diagram of a normal wheel, (c) free-body diagram of a driving wheel.

• Figure shows three states braked, driven and driving.

• Curves represent a given soil strength, tire size, and load. As soil strength increases it moves upward to the left, as it decreases it moves downward to the right.

• Pull and torque are plotted as a function of wheel slip.

---

---

---

---

---

---

---

---

---

---

## Dynamic Traction Ratio

- ✦ Ratio of drawbar pull over dynamic weight on driving wheels
  - will be different for 2-wheel and 4-wheel drive
- ✦ 2-wheel:
  - $DTR2 = F_{db} / (R_{ro} + \Delta R_r)$
- ✦ 4-wheel:
  - $DTR4 = F_{db} / W$
  - $F_{db}$  = drawbar pull (lbs)
  - $R_{ro}$  = static Wt on rear wheel (lbs)
  - $\Delta R_r$  = Wt transfer to rear (lbs)

---

---

---

---

---

---

---

---

---

---

## Tractive efficiency

- ✦  $TE = P_{db} / P_a$ 
  - Def: Fraction of axle power converted to drawbar power
  - $P_{db}$  = drawbar power (HP)
  - $P_a$  = Axle power (HP)
- ✦  $TE = (F_{db} * S_a) / (K_{ip} * P_a)$ 
  - $K_{ip}$  = 3.6 SI ; 375 English
  - High TE achieved by adjusting ballast to optimize travel reduction

---

---

---

---

---

---

---

---

---

---

Figure 16.8

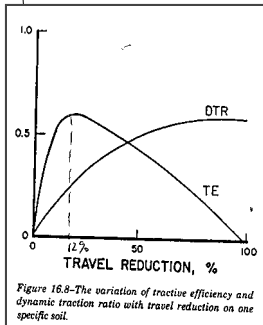


Figure 16.8—The variation of tractive efficiency and dynamic traction ratio with travel reduction on one specific soil.

Goering, Engine and Tractor Power, 1992

- ✦ DTR and TE vary with TR
- ✦ The TR at which peak TE occurs varies depending on track, 4WD, 2WD
- ✦ TR depends on and increases with  $F_{db}$
- ✦ TR at peak TE is least for crawlers, vs highest for 2WD, with 4WD in between.

---

---

---

---

---

---

---

---

---

---

### Tractive Performance and Weight Transfer by ZOZ

- ✦  $\Delta R_r = DWC * F_{db}$ 

$\Delta R_r$ = weight transfer
$F_{db}$ = drawbar force
DWC = dynamic wt. coefficient
- ✦  $DWC = 0.65$  for integral implements mounted to 3-pt hitch
  - $Z_f$  and  $Z_r$  are impractical to measure in field
- ✦  $DWC = 0.45$  semi-mounted implement
- ✦  $DWC = 0.20$  implements on drawbar

---

---

---

---

---

---

---

---

---

---

### Comments on ZOZ chart use

1. Common equations still apply
  - ✦  $TR = [1 - (s_a/s_o)] * 100$  (travel reduction)
  - ✦  $TE = P_{db} / P_a$  (tractive efficiency)
  - ✦  $P_{db} = (F_{db} * s_a) / 375$  (drawbar power)
2. Most specifications are given on concrete track

---

---

---

---

---

---

---

---

---

---

# Comments on ZOZ chart use

- Go to Nebraska tractor test to get vital information on the tractor being evaluated. Such as:
  - SRAF- static rear axle force
  - S<sub>0</sub> -Travel speed with out load
  - P<sub>A</sub> - axle power

## Nebraska Tractor Test Results

**TABLE 16-D. Nebraska tractor test 1992 - International 8400 diesel, 10 speed (cont'd)**

POWER TAKE OFF PERFORMANCE											
Test No.	Speed (km/h)	Power (kW)	Efficiency (%)	Drawbar Pull (kN)	Drawbar Power (kW)	Drawbar Efficiency (%)	Drawbar Speed (km/h)	Drawbar Power (hp)	Drawbar Efficiency (%)	Drawbar Speed (mi/h)	Drawbar Power (hp)
100-20	10.0	100.0	100.0	100.0	100.0	100.0	10.0	100.0	100.0	10.0	100.0
100-25	12.5	100.0	100.0	100.0	100.0	100.0	12.5	100.0	100.0	12.5	100.0
100-30	15.0	100.0	100.0	100.0	100.0	100.0	15.0	100.0	100.0	15.0	100.0
100-35	17.5	100.0	100.0	100.0	100.0	100.0	17.5	100.0	100.0	17.5	100.0
100-40	20.0	100.0	100.0	100.0	100.0	100.0	20.0	100.0	100.0	20.0	100.0
100-45	22.5	100.0	100.0	100.0	100.0	100.0	22.5	100.0	100.0	22.5	100.0
100-50	25.0	100.0	100.0	100.0	100.0	100.0	25.0	100.0	100.0	25.0	100.0
100-55	27.5	100.0	100.0	100.0	100.0	100.0	27.5	100.0	100.0	27.5	100.0
100-60	30.0	100.0	100.0	100.0	100.0	100.0	30.0	100.0	100.0	30.0	100.0
100-65	32.5	100.0	100.0	100.0	100.0	100.0	32.5	100.0	100.0	32.5	100.0
100-70	35.0	100.0	100.0	100.0	100.0	100.0	35.0	100.0	100.0	35.0	100.0
100-75	37.5	100.0	100.0	100.0	100.0	100.0	37.5	100.0	100.0	37.5	100.0
100-80	40.0	100.0	100.0	100.0	100.0	100.0	40.0	100.0	100.0	40.0	100.0
100-85	42.5	100.0	100.0	100.0	100.0	100.0	42.5	100.0	100.0	42.5	100.0
100-90	45.0	100.0	100.0	100.0	100.0	100.0	45.0	100.0	100.0	45.0	100.0
100-95	47.5	100.0	100.0	100.0	100.0	100.0	47.5	100.0	100.0	47.5	100.0
100-100	50.0	100.0	100.0	100.0	100.0	100.0	50.0	100.0	100.0	50.0	100.0

**CLASSIFICATION TABLE FOR THE 1000 SERIES**

Power (kW)	Power (hp)	Speed (km/h)	Speed (mi/h)
100	136	10	6.2
150	203	15	9.3
200	271	20	12.4
250	338	25	15.5
300	406	30	18.6
350	473	35	21.7
400	541	40	24.8
450	608	45	27.9
500	676	50	31.0
550	743	55	34.1
600	811	60	37.2
650	878	65	40.3
700	946	70	43.4
750	1013	75	46.5
800	1081	80	49.6
850	1148	85	52.7
900	1216	90	55.8
950	1283	95	58.9
1000	1351	100	62.0

## ZOZ Chart

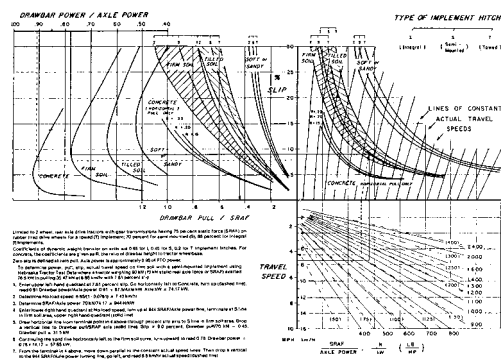


Figure 18-9-Traction prediction chart. (Reprinted from ASAE Data Disk 4, Agricultural machinery management, revised December 1987.)

### Comments on ZOZ chart use

3. If given the percent slip on concrete, enter at the slip in upper quadrant and go to the right to get TE and  $F_{db} / SRAF$
4. Calculate  $S_o$  and  $SRAF / P_a$ , go to bottom right corner. Go up to speed curves, stopping at the right soil and hitch conditions. Follow lines of constant actual speed to get  $S_a$ .

---

---

---

---

---

---

---

---

### Comments on ZOZ chart use

5. Go right to get the percent slip in soil condition
6. Turn down to get  $F_{db} / SRAF$
7. Turn up to get TE

---

---

---

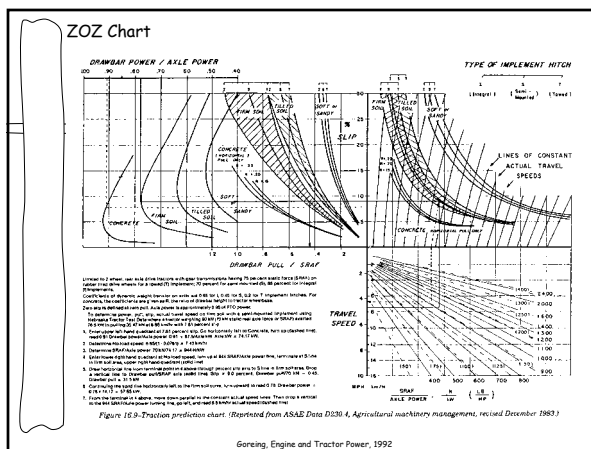
---

---

---

---

---



---

---

---

---

---

---

---

---



## Rolling Resistance

- Force required to keep equipment moving at a constant speed
- Is proportional to equipment weight
- ‡ Coefficient of Rolling Resistance
  - $\rho = F_{\text{draft}} / W_{\text{equip}}$  (English)
  - $\rho = F_{\text{draft}} / (M_{\text{equip}} * 9.807(\text{m/s}^2))$  (SI)
- ‡ % slope =  $\tan$  (angle soil surface and horizontal)

---

---

---

---

---

---

---

---

## Example 1a:

- ‡ A tractor is pulling an 11,000 lb loaded wagon up a 10% slope at 6.2mph. The tractor weight is 6600 lbs.
  - Find the drawbar power if the coefficient of rolling resistance is 0.05 for all wheels.

---

---

---

---

---

---

---

---

Figure 2.3

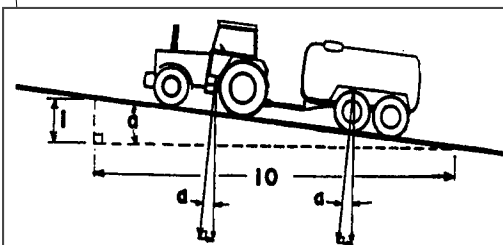


Fig. 2.3. Effects of weight on equipment moving up slope.

Hunt, Farm Power and Machinery Management, 2000

---

---

---

---

---

---

---

---

### Example 1a con't:

1. Angle  $a = \arctan(0.1) = 5.71^\circ$
  2. Components of weight
    - \* Perpendicular to the slope
      - \* Wagon:  $11,000 \cos 5.71^\circ = 10,945 \text{ lbs}$
      - \* Tractor:  $6,600 \cos 5.71^\circ = 6567 \text{ lbs}$
    - \* Parallel to the slope
      - \* Wagon:  $11,000 \sin 5.71^\circ = 1094.4 \text{ lbs}$
      - \* Tractor:  $6600 \sin 5.71^\circ = 656.7 \text{ lbs}$
- \*

---

---

---

---

---

---

---

---

### Example 1a con't:

3. Rolling resistance =  $\rho$  \* wagon perpendicular
  - \* Wagon:  $0.05 * 10945.42 = 547.25 \text{ lbs}$
4. Drawbar Pull = wagon parallel plus rolling resistance
  - $F_{db} = 547.25 + 1094.43 = 1641.68 \text{ lbs}$
5. Drawbar power required
  - $DBP = (1641.68 \text{ lbs} * 6.2 \text{ mph}) / 375 \text{ lbs*mph/HP}$   
 $= 27.14 \text{ HP}$

---

---

---

---

---

---

---

---